

केंद्रक - 055

PHYSICS PAPER - II (NEW) (12126) PHY-122 Theoretical Physics

P. Pages: 3

Time: Two Hours

Max. Marks: 40

Instructions to Candidates:

- Do not write anything on question paper except Seat No.
- Answersheet should be written with blue ink only. Graph or diagram should be drawn with the same pen being used for writing paper or black HB pencil.
- Students should note, no supplement will be provided.
- 4. All questions are compulsory and carry equal marks.
- Figures to right indicate full marks.
- Draw necessary diagrams wherever necessary.
- Use of lograthamic table or electronic calculator is allowed.
- 8. Symbols have their usual meaning.
- Attempt any eight of the following.

8

- a) Add the complex numbers $z_1 = 6 5i$, $z_2 = 3 i$.
- b) Evaluate $\overrightarrow{i} \cdot (\overrightarrow{i} \overrightarrow{k})$
- c) State the de-moivre's theorem mathematical statement.
- d) If $F(x, y) = x^3y^2 e^{xy}$ find F_x , partial derivative.
- e) If z = 2 + 2i determine |z|.
- f) State necessary and sufficient condition of exact differentiation.
- g) If $\phi = \phi(x, y, z)$ define $\overrightarrow{\nabla} \phi$ equation.
- h) State any two examples of vector field
- i) If $\overrightarrow{A} = \overrightarrow{2i} + \overrightarrow{2j} \overrightarrow{k}$ and $\overrightarrow{B} = \overrightarrow{6i} \overrightarrow{3j} + \overrightarrow{2k}$ calculate $\overrightarrow{A} \cdot \overrightarrow{B}$.

2. Attempt any four.

8

- a) if $p + iq = \frac{1+2i}{1-3i}$ find the values of p & q.
- b) Write the complex number $-3i^2 + i$ in standard form.
- c) If $F = x^2 y^2$ and $x = r \cos \theta$, $y = r \sin \theta$ then find $(F_x)_y$.
- d) If $F = x^3y^3 xy^3$ then find F_x , F_y .
- e) Under what conditions the vector field is solenoidal and irrotational.
- f) State physical meaning of grad φ.

Attempt any two.

8

- a) Using Euler's formula obtain trigonometric functions $\sin \theta$, $\cos \theta$, $\csc \theta$
- b) Obtain partial derivatives If F = xy where $x = r \cos \theta$, $y = r \sin \theta$.
- c) Find work done in moving an object along a vector $\overrightarrow{r} = \overrightarrow{i} + 2\overrightarrow{j} \overrightarrow{k}$ and applied force $\overrightarrow{f} = 2\overrightarrow{i} + 3\overrightarrow{j} + 4\overrightarrow{k}$.

4. a) Attempt any two.

6

- i) If $F = \frac{x}{y}$, Prove that $x \frac{\partial F}{\partial x} + y \frac{\partial F}{\partial y} = 0$.
- ii) Determine volume of parallelopiped defined by following three vectors

$$\vec{A}=\vec{i}+\overset{\rightarrow}{2j}-\overset{\rightarrow}{3k}$$

$$\overrightarrow{B} = \overrightarrow{i} + \overrightarrow{k}$$

$$C = \overrightarrow{i} - 2\overrightarrow{k}$$

- iii) Show that $\nabla \cdot \nabla \varphi = \nabla^2 \varphi$
- b) Find the real number x and y for which (x + 2i)(1-i) = 5 + iy.

2

5. a) Attempt any one.

6

- i) Explain vector triple product.
- ii) Define grad ϕ , div \overrightarrow{V} and carl \overrightarrow{V} , State physical significance of each in brief.
- b) Express $z = \sqrt{2}i$ in polar form.

2
